

ASP-DAC 2022

Differentially Evolving Memory Ensembles

Pareto Optimization based on Computational Intelligence for
Embedded Memories on a System Level

Felix Last, Ceren Yeni & Ulf Schlichtmann



intel®

Technische
Universität
München



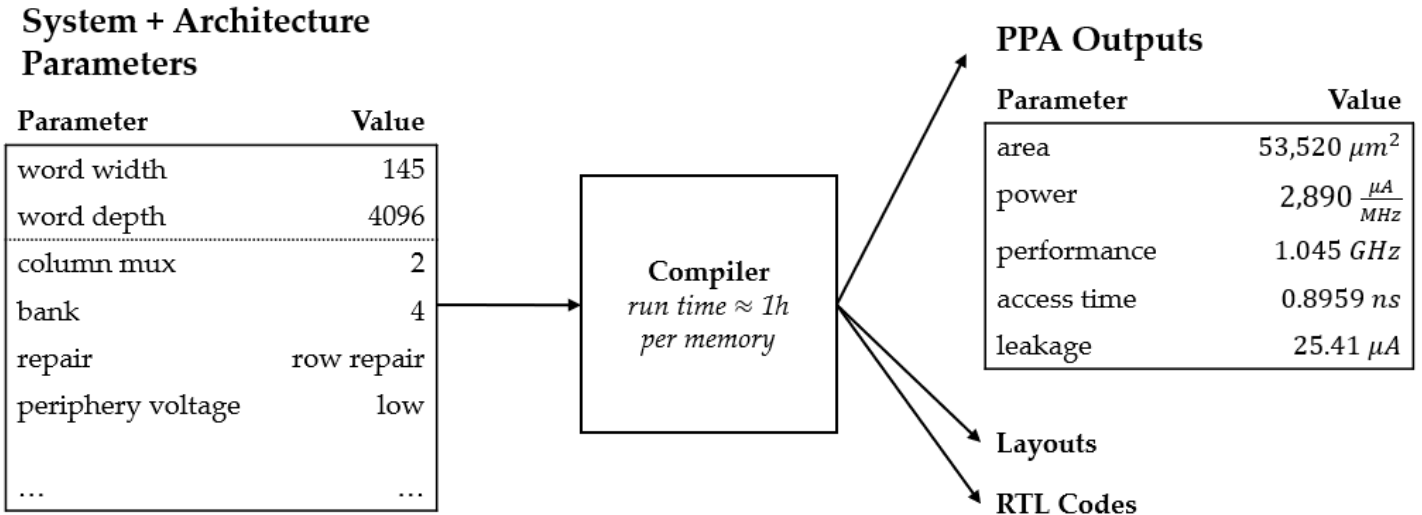
TUM

Agenda

- I. Motivation
- II. Proposed Method
 - I. Algorithm Choice
 - II. Differential Evolution
 - III. Feasibility Repair
 - IV. NSGA-II Selection
- III. Results
- IV. Conclusion & Outlook

Motivation (1/2)

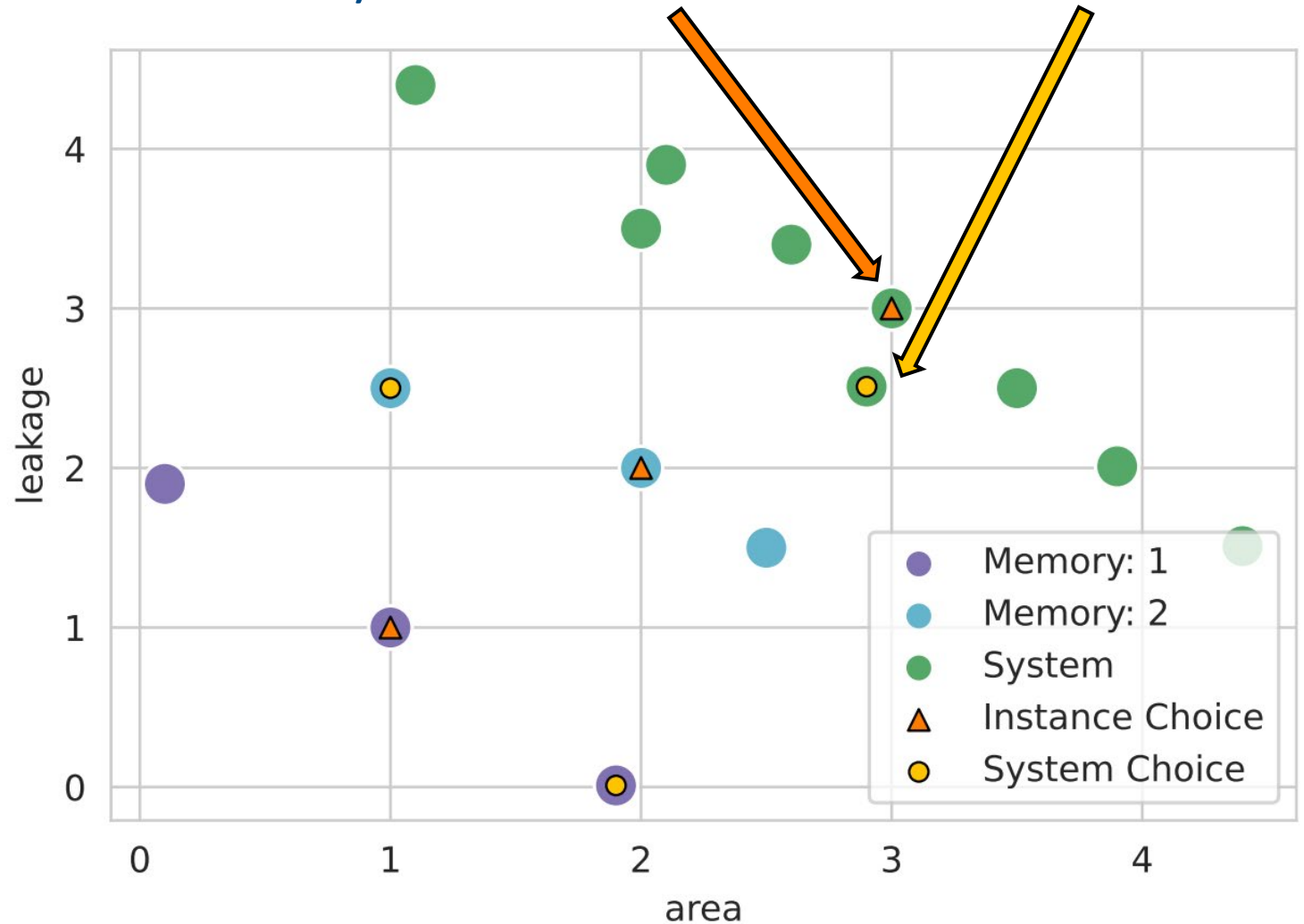
- Memory compilers generate embedded memories
- Architectural parameters require “knob-tuning”
- Conflicting objectives: power, performance, and area (PPA)
- Modern ICs contain 500-10,000 memories → substantial PPA impact
- Feasibility constraints



Motivation (2/2)

- Consider the combinatorial Pareto front on system level
- System-level optimization may yield better choice than sequential instance optimization

The result of choosing the... is objectively dominated on the system level.
balanced trade-off per memory instance...



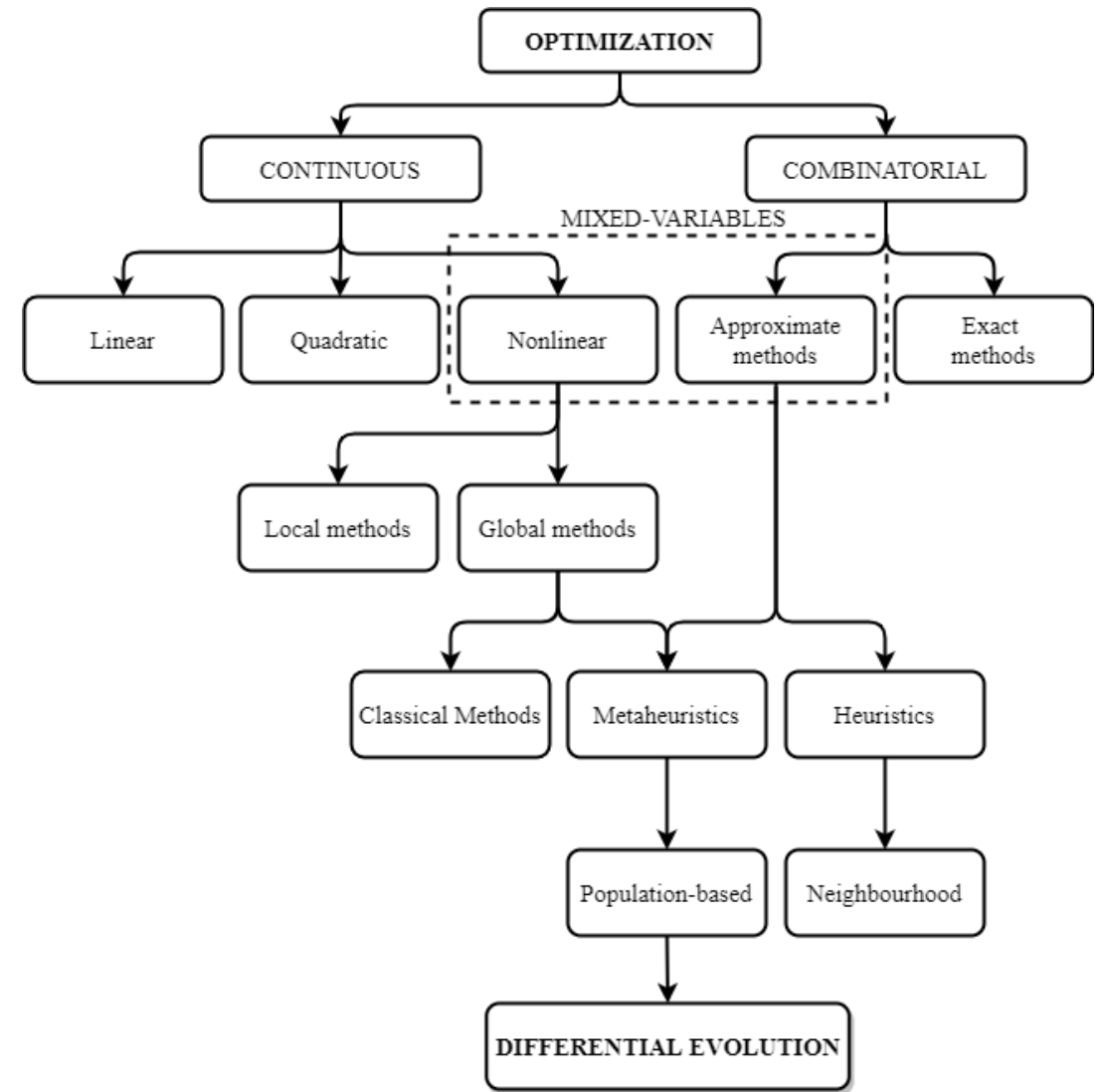
Proposed Method (1/4)

- Algorithm selection from 40 choices through requirement-traceability matrix
- Match problem characteristics to algorithm characteristics

Optimization algorithm selection requirement traceability matrix																
Characteristics required for the problem	multi objective optimization	discrete variable values	continuous objective function	high dimensional solution vector	convergence to global optimum	computationally inexpensive	non-convex problem	fast convergence	non-linear functions	robustness	stability	stochastic methods	scalability	good exploration of the design space	executable in parallel	Score
Importance	3	1	2	3	1	0	1	3	1	2	1	2	3	2	3	-
Differential evolution (DE)	1	1	1	1	1		1	1	1	1		1	1		1	25
Artificial bee colony (ABC)	1	1	1		1		1	1	1	1		1		1		18
Ant colony optimization	1	1		1	1		1	1	1					1		15
Bat algorithm (BA)	1	1	1		1		1		1	1	1			1		14
Artificial fish swarm (AFS)	1	1	1		1		1		1	1				1		13
Particle swarm optimization (PSO)	1	1	1	1											1	12
Cuckoo search (CS)	1	1	1					1	1							10
Genetic algorithm (GA)	1	1			1		1		1			1				9

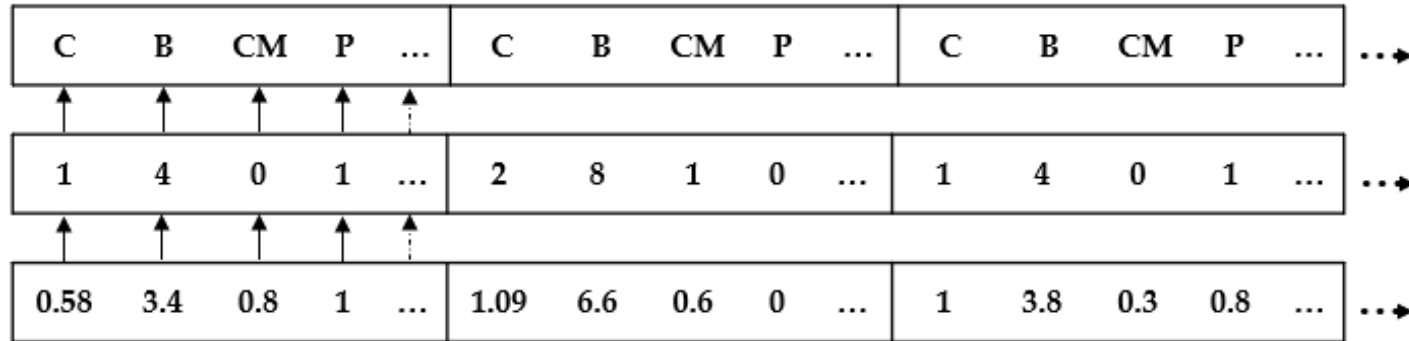
Proposed Method (2/4)

- Differential Evolution
 - evolutionary algorithm
 - metaheuristic
 - population-based
 - global
 - few control parameters



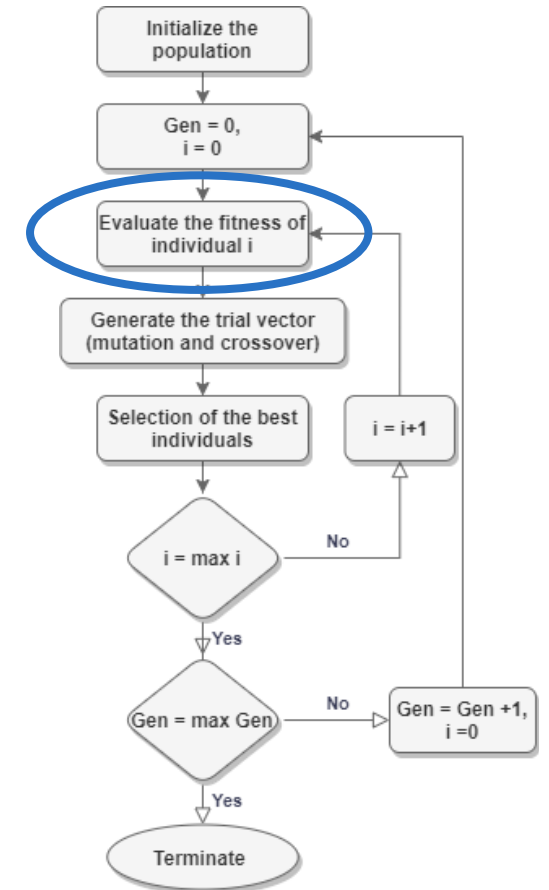
Proposed Method (3/4)

Repairing individuals to feasible compiler parameters:



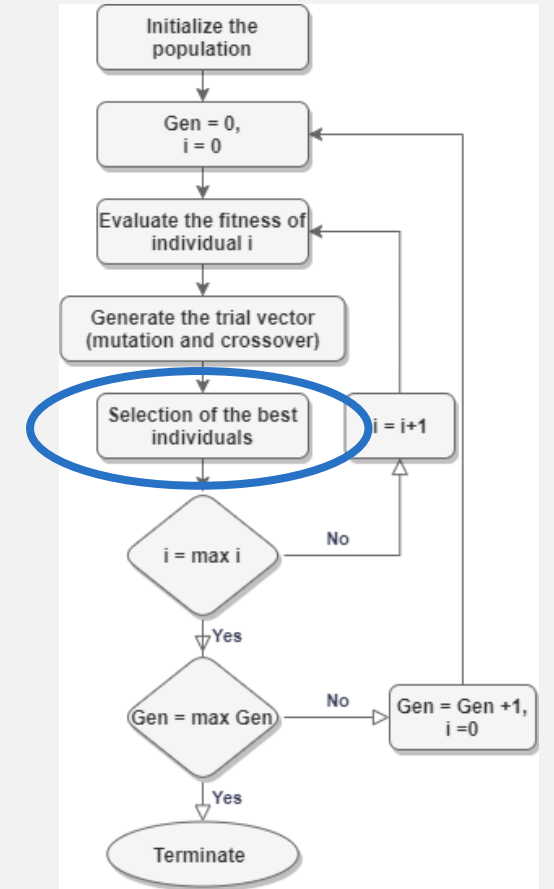
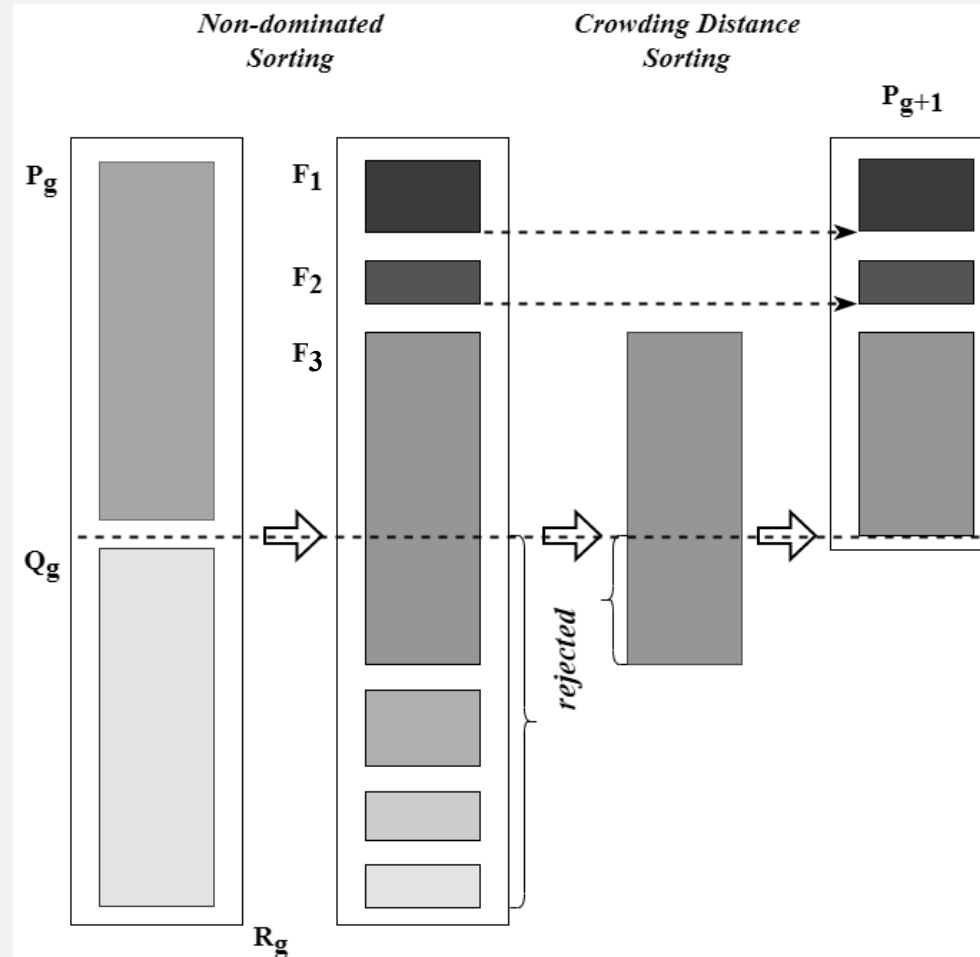
A look-up table for the transformation of the parameters:

Compiler	V_{th}	$\overline{V_{th}}$
compiler A	low-vt	0
compiler A	standard-vt	1
compiler A	high-vt	2
compiler B	low-vt	0
...



Proposed Method (4/4)

- Selection based on Pareto dominance through NSGA-II
- Non-dominated sorting & crowding distance sorting



Results (1/4)

- Experimental Setup
 - Two systems (A, B)
 - System size: 4 memories
 - Design space per memory: 50-900 candidates
 - System design space: >500M combinations
- Small systems allow exhaustive combinatorial search
 - “Golden baseline”
 - Infeasible for larger systems

Results (2/4)

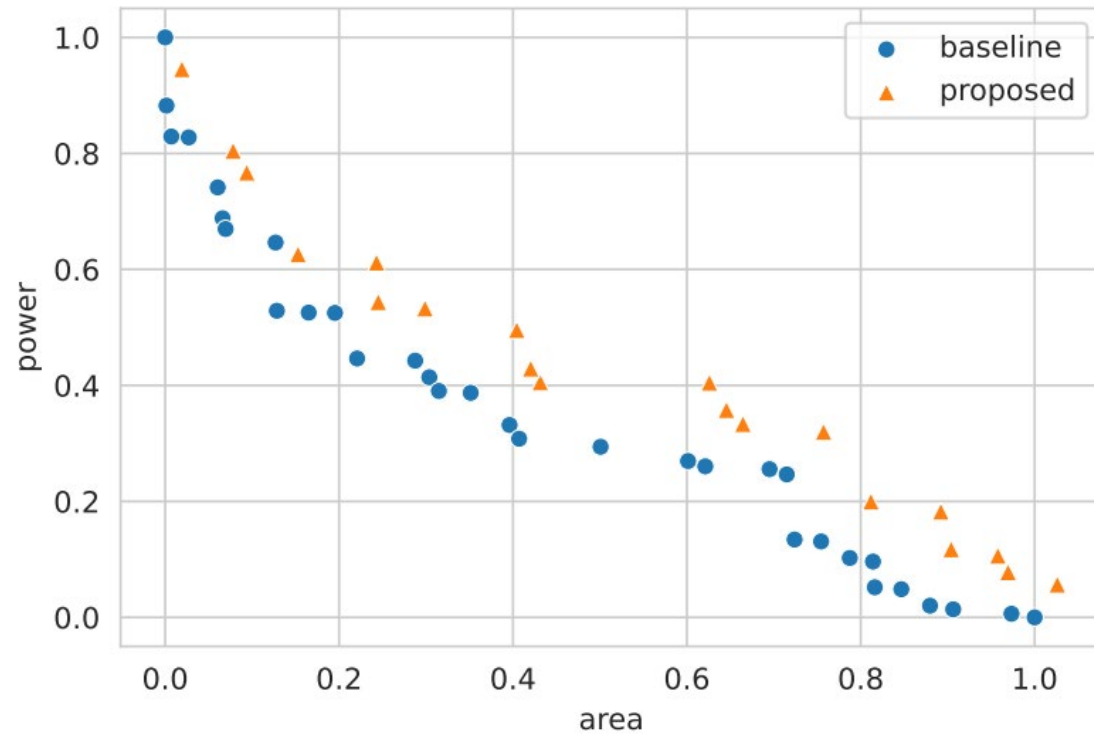
Two main control parameters of differential evolution:
Differentiation constant F ; crossover constant CR

Test Case No.	F	CR	NP	No. of Generations	Area [μm^2]			Power [$\mu A/MHz$]		
					min	max	mean	min	max	mean
1	0.4	0.5	10	20	169.390	172.477	170.770	4.289	4.433	4.369
2	0.8				164.405	174.305	168.910	4.231	4.409	4.322
3	1.2				163.431	172.311	167.992	4.216	4.349	4.285
4	0.4	0.7			166.194	173.493	170.945	4.246	4.386	4.292
5	0.8				167.508	178.270	172.003	4.285	4.506	4.394
6	1.2				168.439	180.569	172.514	4.298	4.471	4.368
7	0.4	0.9			170.925	176.770	174.107	4.303	4.432	4.357
8	0.8				167.378	176.409	172.200	4.284	4.461	4.374
9	1.2				168.554	177.227	173.326	4.333	4.512	4.402

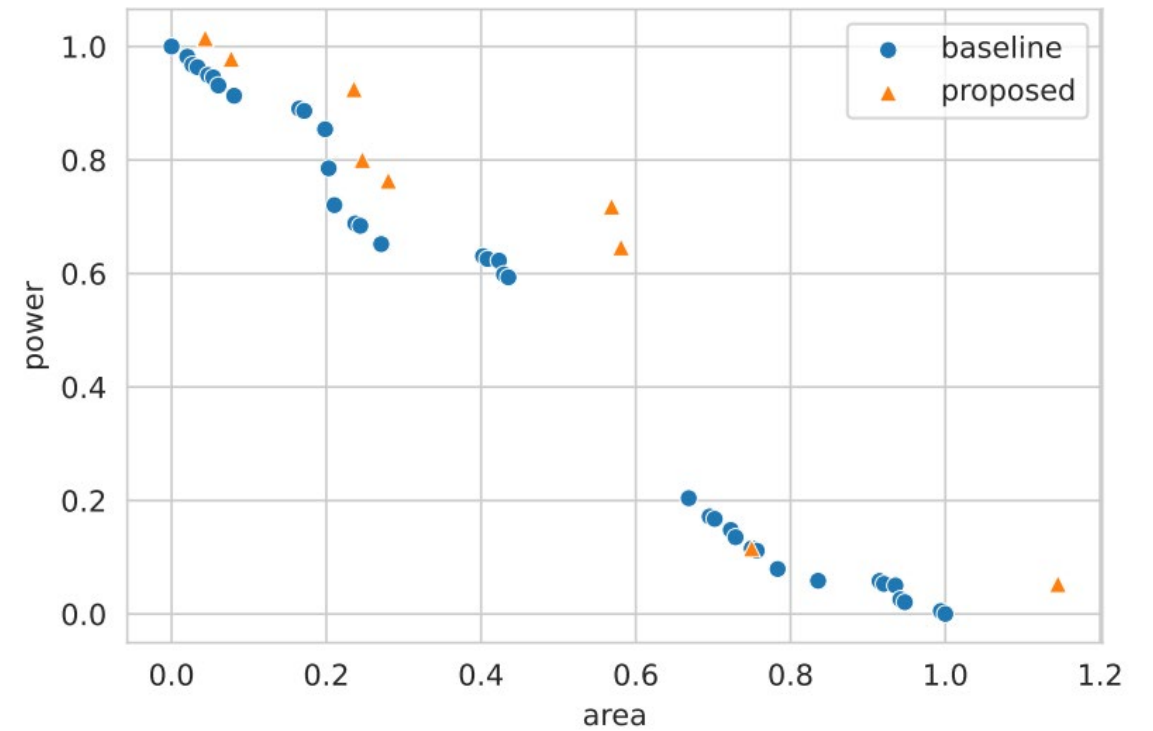
Results (3/4)

Pareto fronts found by proposed method and “golden baseline” for two systems of memories

■ System A



■ System B



Results (4/4)

Performance indicators for System A

	Exhaustive Search	Proposed Method
# solutions evaluated	644,972,544	2,000
RAM Usage	>100GB	<<1GB
Runtime	20min	9min
Feasibility	Small systems only	Scalable to large systems
Distance from best area	0%	0.54%
Distance from best power	0%	0.75%

Conclusion & Outlook

- Proposed method: Differential Evolution + NSGA-II selection
- Enablement of system optimization – previously infeasible
- $< 0.55\%$ distance from best area, $< 0.75\%$ from best power

- Incorporation of hard constraints on the objective function values
- Dynamic adjustment of control parameters
- Perform experiments on large-scale problems
- Study effect of repair on diversity